

## Time to Event Data

### Survival Analysis

Methods for examining time to occurrence of event, often death or morbidity  
(e.g. cancer recurrence, MI)

Times measured from defined time origin (usually subject specific)

- definition depends on purpose

Censored observations: subjects where follow-up ends before occurrence of event due to:

- end of pre-determined follow-up

- unintended loss to follow-up

In absence of censoring, can easily plot survival curve

y = (decreasing) proportion of subjects still "event-free"

x = follow-up time

Allowing for censoring?

large samples - life table approach

smaller samples - Kaplan Meier curve.

Hazard rate at time t = probability that an event occurs (given subject hasn't already had the event).

Estimated as  $\frac{\# \text{ experiencing event at time } t}{\# \text{ still event free up to time } t} = \frac{\# \text{ events}}{\# \text{ at risk of event}}$

- can be calculated even in presence of censoring

Constructing the survival curve:

$S(t)$  (the survival function) = probability of survival (proportion surviving) up to time t

If events can occur at  $t_1, t_2, t_3, \dots, t_i$ ,  $S(t)$  can be expressed as

$$S(t_i) = [1 - h(t_1)] \times [1 - h(t_2)] \times [1 - h(t_3)] \times \dots \times [1 - h(t_i)]$$

$\hat{S}(t_i)$  derived by estimate h's as proportion in relative "risk set"

## Plotting a Survival Curve, $\hat{S}(t)$

- steps occur at "events"
- censoring times often indicated with "|"s
- provides a valid estimate of true "uncensored" survival curve if censoring is independent of event (non-informative censoring)

## Comparing Survival Curves

Graphical: superimposed Kaplan-Meier curves for two groups

Formal test of hypothesis: Log-rank test (variant of Mantel-Haenszel, time as stratifying variable)

## Assumptions of the Log-Rank test

Independent samples of survival data

Non-informative censoring in both samples (but may not be "uniform")

Proportional hazards assumption

Consider TRUE hazard function  $h_i(t)$  for group  $i$  ( $i = 1, 2$ )

$$\frac{h_1(t)}{h_2(t)} = \lambda, \text{ same value for all values of } t.$$

$\lambda$  is "relative hazard" - similar to relative risk

## Log-rank test

Based on above assumptions, test  $H_0: \lambda = 1$

$O$  = observed number deaths in one group (e.g. Group 1)

$E$  = expected number, based on follow-up pattern

$V$  = variance of  $O$  (messy)

$$X^2 = \frac{(|O - E| - .5)^2}{V} \text{ refer to } \chi^2 \text{ on 1 degree of freedom}$$

## Checking assumptions

Informal: Check for "parallel" pattern in survival curves

Log-log plot: Plot of  $-\log_e[\log_e(\hat{S}(t))]$  versus  $\log_e(t)$

- improves visual acumen